

NEW ZEALAND OUALIFICATIONS AUTHORITY MANA TOHU MÁTAURANGA O AOTEAROA

Level 3 Calculus, 2007

90638 Manipulate real and complex numbers, and solve equations

Credits: Five 2.00 pm Thursday 22 November 2007

Check that the National Student Number (NSN) on your admission slip is the same as the number at the top of this page.

Make sure you have a copy of the Formulae and Tables Booklet L3-CALCF.

You should answer ALL the questions in this booklet.

Show ALL working for ALL questions.

If you need more space for any answer, use the page(s) provided at the back of this booklet and clearly number the question.

Check that this booklet has pages 2–8 in the correct order and that none of these pages is blank.

YOU MUST HAND THIS BOOKLET TO THE SUPERVISOR AT THE END OF THE EXAMINATION.

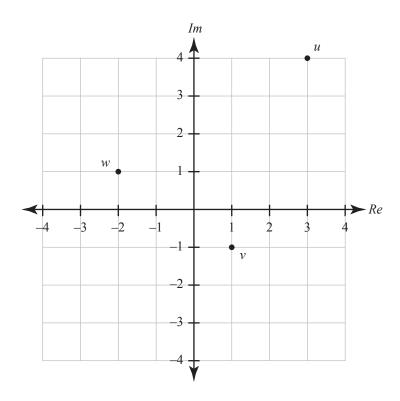
For Assessor's Achievement Criteria			
Achievement	Achievement with Merit	Achievement with Excellence	
Manipulate real and complex numbers, and solve equations.	Solve more complicated equations.	Solve problem(s) involving real or complex numbers.	
Overall Level of Performance			

90638

You are advised to spend 40 minutes answering the questions in this booklet.

QUESTION ONE

The complex numbers *u*, *v* and *w* are shown on the Argand diagram below.



Write each of the following as a complex number in rectangular form, a + bi.

(a) w - u

(b) $\frac{u}{v}$

QUESTION TWO

p and *q* are complex numbers, where $p = 2 \operatorname{cis} \frac{\pi}{4}$ and $q = 6 \operatorname{cis} \frac{3\pi}{7}$. Find *pq*, expressing your answer in polar form, $r \operatorname{cis} \theta$.

QUESTION THREE

Write $(3+\sqrt{2})(7-\sqrt{2})$ in the form $a+b\sqrt{2}$, where a and b are rational numbers.

Assessor's use only

Assessor's use only

QUESTION FOUR

Solve the following equations for x, expressing the solutions in their simplest form.

(a) $x^2 - 4ax + a^2 = 0$

(b) $\log_3(4-5x) = 6$

QUESTION FIVE

Solve the following equation for x in terms of p.

$$2\sqrt{x+1} - p\sqrt{x} = 0$$

QUESTION SIX

Solve the following equation for x in terms of q.

 $2^{3x-1} = 7^{x-q}$

QUESTION SEVEN

Solve $z^4 = 16 \operatorname{cis} \frac{2\pi}{5}$, where z is a complex number.

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Write your answers in polar form, $r \operatorname{cis} \theta$.

Find the equation of the locus of the point representing z if |z - 3i| - |z + 3i| = 2.

7

Assessor's use only

Extra paper for continuation of answers if required. Clearly number the question.

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Question number